

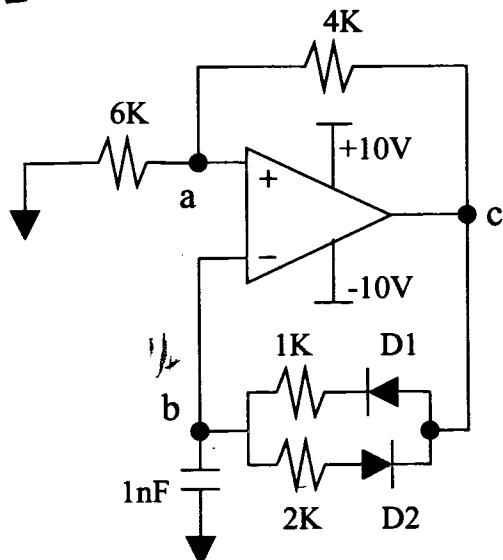


papers if needed.)

(37/60)

Questions 1: (20marks)

For the circuit below, make appropriate assumptions, sketch the waveforms at the op-amp terminals (i.e., node a, b, c).

Assume Ideal op-amp

$$a = v_+ = \frac{R_f}{R_i + R_f} v_o$$

(12)

Assume C initially uncharged

Charging

$$v_b = 12 - (12 - (-12 + v_d)) e^{-\frac{t}{RC}} \text{ use } R = 2k\Omega \text{ current will flow from } b \rightarrow C.$$

$$= 12 - (24 - V_d) e^{-\frac{t}{(2k)(1 \times 10^{-9})}} \text{ when } t = t_1, V_b = 12V - V_d$$

$$12V - V_d = 12 - (24 - V_d) e^{-\frac{t_1}{(2k)(1 \times 10^{-9})}}$$

$$\frac{V_d}{24 - V_d} = e^{\frac{-t_1}{(2k)(1 \times 10^{-9})}}$$

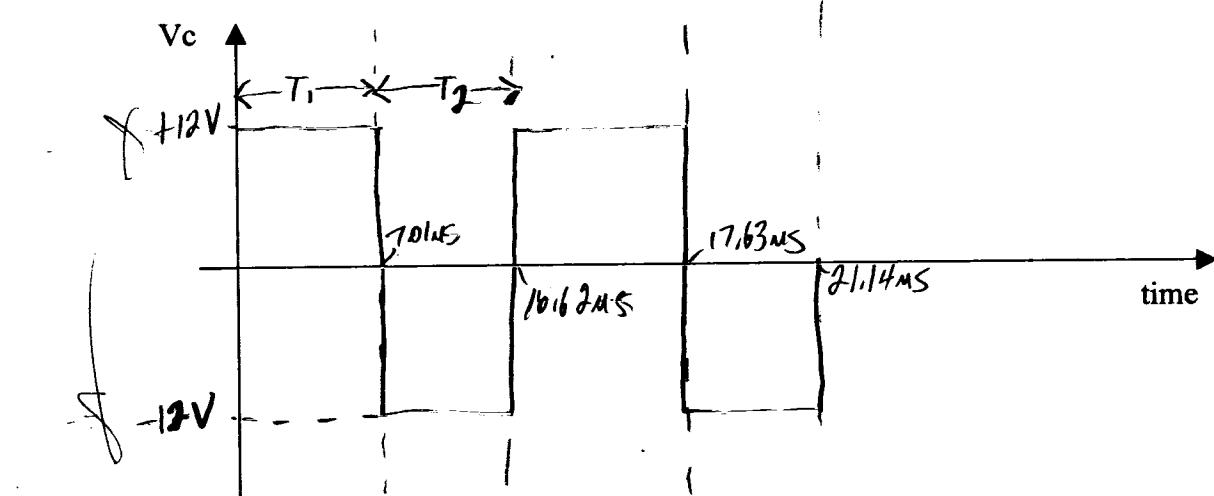
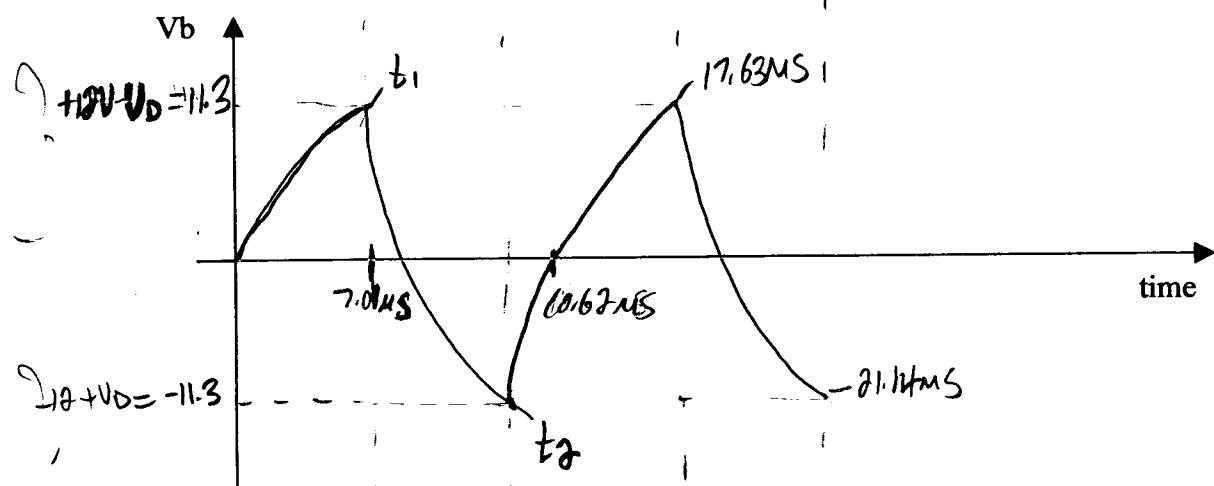
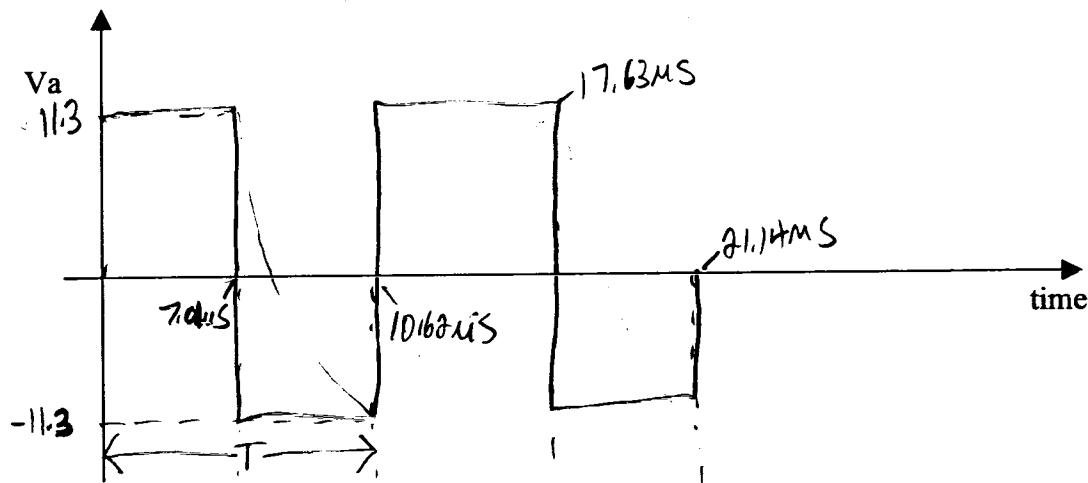
$$\frac{t_1}{2k(1 \times 10^{-9})} = \ln\left(\frac{24 - V_d}{V_d}\right)$$

$$t_1 = 7.01 \mu s$$

In our case $t_1 \neq t_2$ b/c of different R b/w b & C.

$$t_2 = (1k)(1 \times 10^{-9}) \ln\left(\frac{24 - V_d}{V_d}\right) = 3.51 \mu s$$

$$\tau = 7.01 \mu s + 3.51 \mu s = 10.62 \mu s$$



Question 2: (30marks)

Part 1:

An op-amp has the following open-loop transfer function:

$$A(j\omega) = \frac{v_{out}}{v_{in}} = \frac{10^5}{(1+j\frac{\omega}{\omega_1})(1+j\frac{\omega}{\omega_2})(1+j\frac{\omega}{\omega_3})}$$

where $\omega_1 = 100\text{rad/s}$, $\omega_2 = 10^3\text{rad/s}$, and $\omega_3 = 10^5\text{rad/s}$.

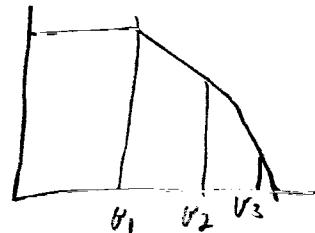
X If the op-amp is connected in a unity positive feedback configuration. What is the output frequency of the op-amp?

$A(j\omega)=1$ in unity feedback

$$10^5 = \left(1 + j\frac{\omega}{\omega_1}\right) \left(1 + j\frac{\omega}{\omega_2}\right) \left(1 + j\frac{\omega}{\omega_3}\right)$$

$\omega > \omega_3$ when gain=1

$$\boxed{\omega \approx 87000\text{rad/s}}$$



X If the op-amp is to be connected in a negative feedback configuration. What is the maximum feedback coefficient that can be tolerated before instability results? What is the minimum closed-loop gain of this op-amp without oscillation?

Find ω

$$-180^\circ = -\tan^{-1}\left(\frac{\omega}{100\text{rad/s}}\right) - \tan^{-1}\left(\frac{\omega}{10^3\text{rad/s}}\right) - \tan^{-1}\left(\frac{\omega}{10^5\text{rad/s}}\right)$$

$$\omega_{180} = 65928.55\text{rad/s}$$

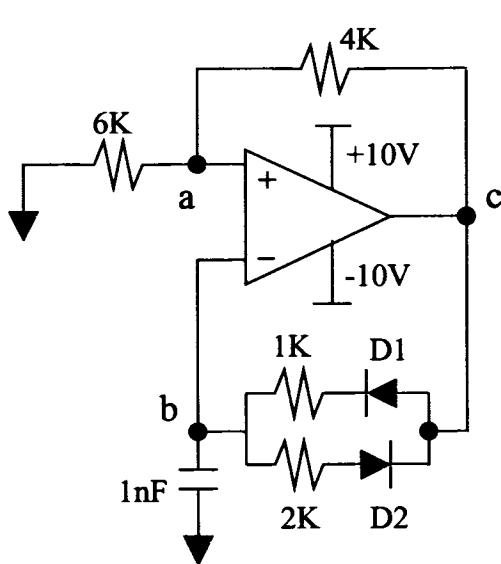
$$A|_{180} = \left| \frac{10^5}{\left(1 + j\left(\frac{65929}{100}\right)\right) \left(1 + j\left(\frac{65929}{1000}\right)\right) \left(1 + j\left(\frac{65929}{100000}\right)\right)} \right| = 1.97 \approx 2$$

$$B \leq \frac{1}{2} = 0.5$$

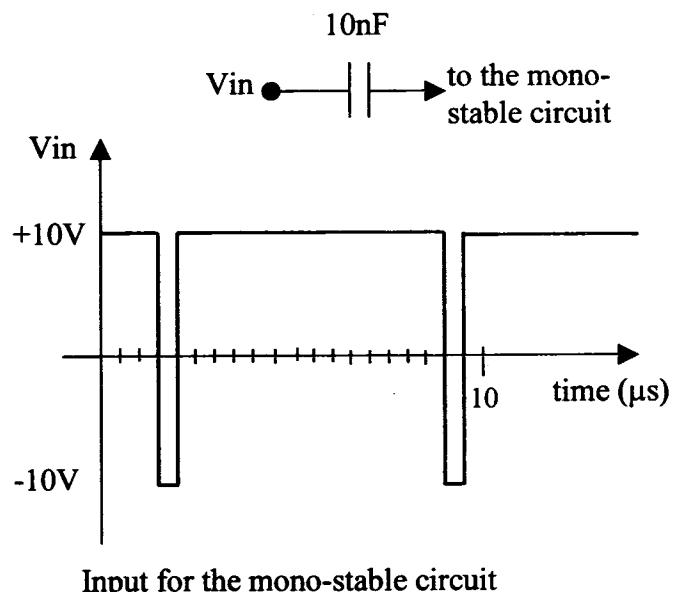
$$\boxed{A_{CL} \geq 2}$$

Part 2:

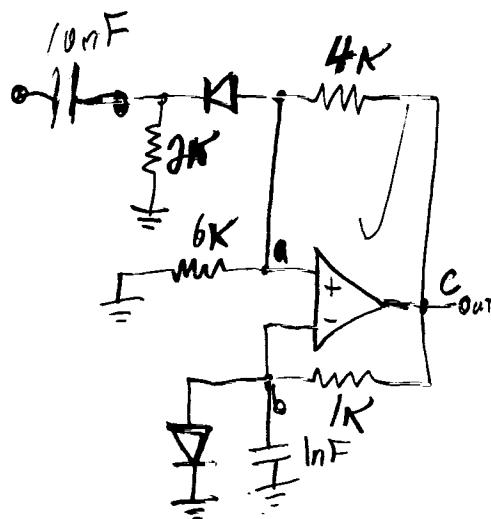
The circuit in Question 1 is shown below (a); without adding or deleting any component, rearrange the circuit to make it function as a mono-stable circuit. Connect your circuit to the input Vin given in (b), sketch the waveforms at the op-amp terminals a, b, c of your modified circuit.



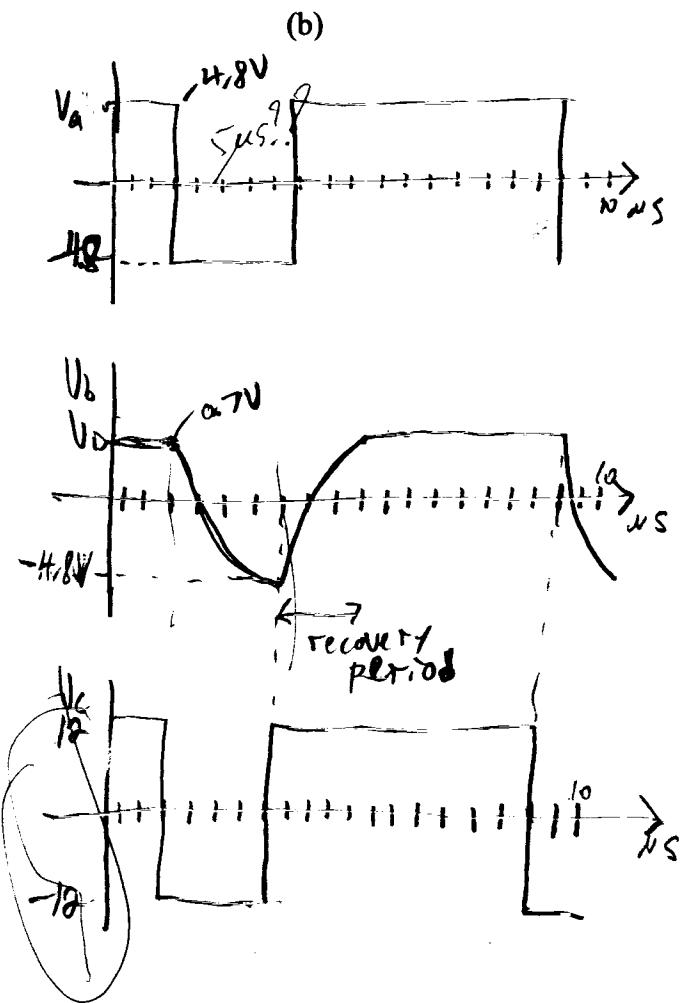
(a)



Input for the mono-stable circuit

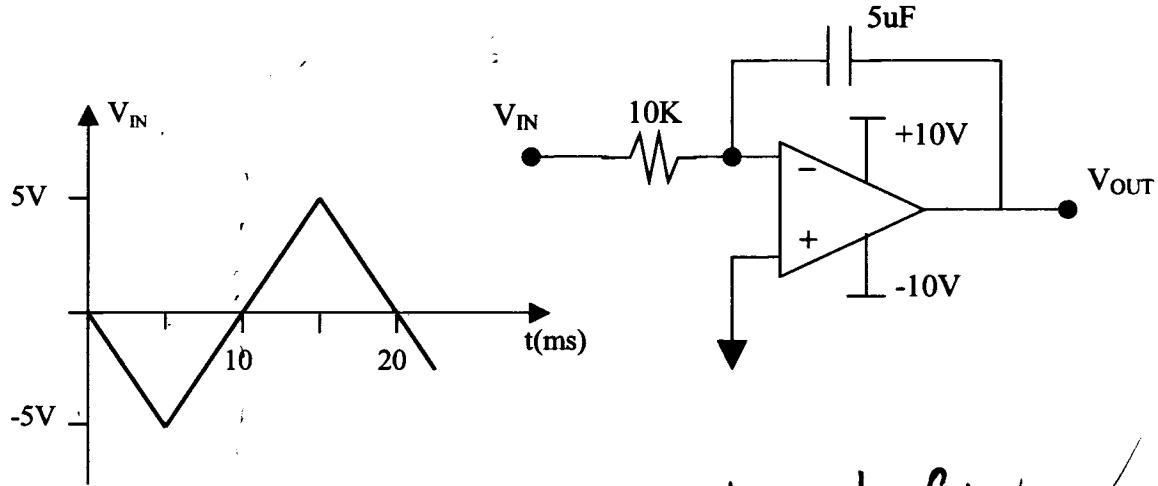


$$BL+ = \frac{4.8}{10M} (12) = +4.8V$$

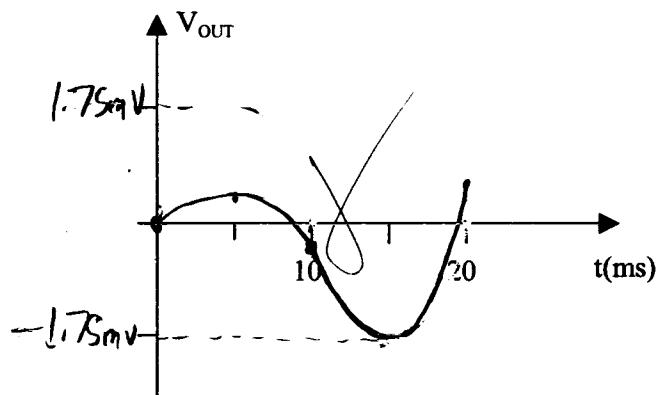


Question 3: (10marks)

A 5V peak triangular voltage with a period of 20ms, depicted on the axis shown below, is applied to an ideal op-amp integrator. Sketch V_{OUT} as a function of time. The capacitor has zero initial charge.



$$V_o = -\frac{1}{RC} \int V_i dt$$



b/w 0-5

$$V_o = -\frac{1}{RC} \int_{0ms}^{5ms} -t dt = +\frac{1}{RC} \frac{1}{2} t^2 \Big|_{0ms}^{5ms}$$

$$= \frac{1}{RC} \frac{1}{2} \frac{(5ms)^2}{(0.1s)(5 \times 10^{-3})} = 0.25mV$$

$$\text{at } t = 5ms \quad V_{out} = 0.25mV$$

$$\text{at } t = 10ms \quad V_{out} = -0.5mV$$

b/w 5-15ms

$$V_o = -\frac{1}{RC} \int_{5 \times 10^{-3}}^{15 \times 10^{-3}} t dt + V_{out} = \frac{-1}{(0.1s)(5 \times 10^{-3})} \frac{1}{2} t^2 \Big|_{5ms}^{15ms} + 0.25mV = -1.75mV$$

$$\text{at } t = 15ms \quad V_{out} =$$

b/w 15ms-20ms

$$V_o = -\frac{1}{RC} \int_{15ms}^{20ms} -t dt + V_o = +\frac{1}{(0.1s)(5 \times 10^{-3})} \frac{1}{2} t^2 \Big|_{15ms}^{20ms} - 1.75mV = 0$$

